



DAE Mobile Training Team

RANDOM FAILURE
(Weibull's Distribution)

TEST & TUTORIAL

As of 5th Feb 2021



แบบทดสอบ RANDOM FAILURES (Weibull' Distribution)

แบบทดสอบ RANDOM FAILURE (WEIBULL'S DISTRIBUTION)

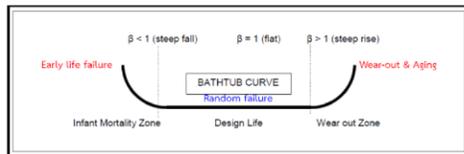
1. According to reliability engineers, which of the following is true ?

- a. Weibull analysis is the implied assumption that the future is the same as the past.
- b. As soon as design, maintenance or operating policies and practices change, the prior failure history becomes unrepresentative of the future.
- c. Weibull Analysis requires complete and accurate failure data over a period of stable practices.
- d. All of the above a, b and c are true.

2. According to Weibull data, which of the following is NOT true ?

- a. Complete data is the practitioner is aware of the exact time-to-failure for a sample of the product.
- b. Right Censored data is that all population failed at exact time.
- c. Left Censored data is that the failures are between 0 and 50 hours.
- d. All of the above a, b and c are not true.

3. Use the Bathtub Curve to choose the correct answer.



Infant mortality zone is the zone with shape parameter (β) < 1.0; what is the probable cause of infant mortality ?

- a. Inadequate burn in (run in).
- b. Misassemble.

- c. Some quality problems.
- d. All of the above a, b and c are correct.

4. Useful life or design life zone is the zone with shape parameter (β) = 1.0; called for random failures; what is the probable cause of random failures ?

- a. Maintenance errors.
- b. Operating errors.
- c. Failures due to nature (FOD, Lightning Strike,).
- d. All of the above a, b and c are correct.

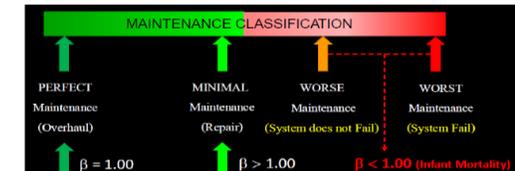
5. Early wear-out zone is the zone with shape parameter $1.0 < \beta < 4.0$; what is the probable cause of early wear out ?

- a. Many mechanical failure modes.
- b. Roller and / or Bearing failures.
- c. V - Belt failures.
- d. All of the above a, b and c are correct.

6. Old age or rapid wear-out zone is the zone with shape parameter $\beta > 4.0$; what is the probable cause of early wear out ?

- a. Stress corrosion.
- b. LCF (Low Cycle Fatigue), HCF (High Cycle Fatigue, TMF (Thermal Fatigue).
- c. Erosion.
- d. All of the above a, b and c are correct.

7. From the maintenance classification figure below, what is the cause of "Worst Maintenance" causing infant mortality ($\beta < 1.0$) ?



- a. Bad maintenance.
- b. Hidden faults.
- c. Human errors and / or use of faulty parts.
- d. All of the above a, b and c are correct.

8. When $\beta = 1.0$, the part implies random failure; overhaul the part is not appropriate for random failure due to independent of time. What type of maintenance is the most effective for parts which have random failures characteristic ?

- a. On Condition (OC)
- b. Condition Monitoring (CM)
- c. System Rate Monitoring (SRM)
- d. Component Reliability Monitoring (CRM)

9. Any Time Change Item (TCI) has its failure rate (λ) = 1 / TBO (Time Between Overhaul). If part "A" has TBO = 2,500 flying hours, what is the failure rate (λ) of part "A" ?

- a. $\lambda_A = 0.0002$ (1/5,000)
- b. $\lambda_A = 0.00025$ (1/4,000)
- c. $\lambda_A = 0.0004$ (1/2,500)
- d. $\lambda_A = 0.0005$ (1/2,000)



แบบทดสอบ RANDOM FAILURES (Weibull' Distribution) Cont.

10. Any Time Change Item (TCI) has its failure rate (λ) = 1 / TBO (Time Between Overhaul).
 Given the design reliability of any part is derived from the formula $R(t) = e^{-\lambda \cdot t}$; t = time.
 Then, the design reliability of any TCI at the expired date ($t = TBO$) shall be
 $R(t)_{TCI \text{ expired date}} = e^{-(1/TBO \cdot TBO)} = e^{-1}$. If e = the base for natural logarithms = 2.718281828...
 What is the reliability of any TCI at its expired date ?

- a. $1/2.718281828 = 0.37$
- b. $(1 - 1/2.718281828) = 0.63$
- c. $(1/2.718281828) \cdot 2 = 0.74$
- d. $(1/2.718281828) \cdot 1.5 = 0.56$

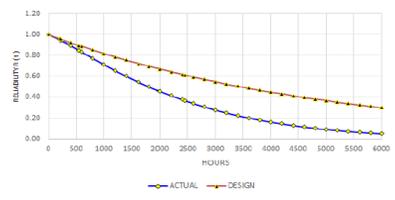
11.

SUMMARY OUTPUT										
Regression Statistics										
Multiple R	0.985491922									
Adjusted R Square	0.979377499									
Standard Error	0.252199491									
Observations	31									
ANOVA										
	df	SS	MS	F	Significance F					
Regression	1	42.13991221	42.13991221	1,226.832777	6.5137E-20					
Residual	29	9.90894762	0.341688194							
Total	30	52.04886983								
	Confidence Interval	Standard Error	t Stat	P-value	Lower 95%	Upper 95%	Lower 95.0%	Upper 95.0%	Lower 99.0%	Upper 99.0%
Intercept	2.460131724	0.244380754	10.06813706	2.98E-20	1.963161266	2.957102184	1.963161266	2.957102184	1.982153331	2.982153331
X Variable 1	1.215811106	0.034200367	35.54929381	6.5137E-20	1.147119062	1.282503151	1.147119062	1.282503151	1.182153331	1.382153331
Total (or Shape Parameter) =	1.215811106									
Alpha (or Characteristic Life) =	2456.222197									

By using Weibull distribution from the figure above, we obtain the value of Shape Parameter (β) = 1.2148 and the value of Characteristic Life (α) = 2,456 flying hours. Which of the following statement is true ?

- a. The part is normal early wear out ($1.0 < \beta < 4.0$). At 2,456 flying hours, 63 % of the part would be failed and 37 % would be good.
- b. The part is normal early wear out ($1.0 < \beta < 4.0$). At 2,456 flying hours, 37 % of the part would be failed and 63 % would be good.
- c. The part is old age wear out ($\beta = 1.2148$). At 2,456 flying hours, 63 % of the part would be failed and 37 % would be good.
- d. The part is old age wear out ($\beta = 1.2148$). At 2,456 flying hours, 37 % of the part would be failed and 63 % would be good.

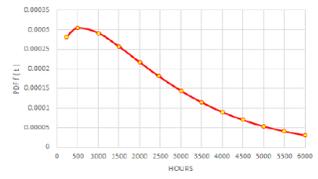
12.



A Time Change Item (TCI) part has its design reliability (orange line) and actual reliability (blue line) as shown in the figure above. The overhaul interval of this TCI part is 5,000 flying hours. What is the reliability of this TCI at 5,000 flying hours expired ?

- a. 0.74
- b. 0.37
- c. 0.63
- d. 0.56

13. PDF f(t) or Population Density Function of a part has its maximum value at 500 flying hours which has reliability = 0.000304 as shown in the figure below. Which of the following statement is correct ?



- a. The part would mostly failed at 500 flying hours.
- b. At 500 flying hours, 37 % of the part would be failed and 63 % would be good.
- c. At 500 flying hours, 63 % of the part would be failed and 37 % would be good.

d. The part would need to be overhauled at 500 flying hours.

14. What shall we do with parts which have been verified as "Infant Mortality ($\beta < 1.0$)" ?

- a. Inform MRO provider or MRO supplier of the situation to find root cause(s).
- b. Inform MRO's Thai Agent of the situation.
- c. Supply Division and Technical Division record and continue to monitor the situation.
- d. All of the above a, b and c are correct.

15. Ideally, how many data points are required regarding Weibull distribution in order to ensure a robust analysis ?

- a. 5 or more data points.
- b. 10 or less data points.
- c. 10 or more data points.
- d. 5 or less data points.



แบบทดสอบ RANDOM FAILURE (WEIBULL'S DISTRIBUTION)

1. According to reliability engineers, which of the following is true ?

- a. Weibull analysis is the implied assumption that the future is the same as the past.
- b. As soon as design, maintenance or operating policies and practices change, the prior failure history becomes unrepresentative of the future.
- c. Weibull Analysis requires complete and accurate failure data over a period of stable practices.
- d. All of the above a, b and c are true.



Weibull Concept

- ◆ Weibull analysis is the implied assumption that the future is the same as the past.
- ◆ As soon as design, maintenance or operating policies and practices change, the prior failure history becomes unrepresentative of the future.
- ◆ An analysis using the old data would produce poor decisions in that case.
- ◆ Weibull Analysis requires complete and accurate failure data over a period of stable practices, along with an analyst who has thorough understanding of the effects of past and current maintenance and operating policies and practices.

เป็นองค์กรที่มุ่งเน้นการพัฒนาระบบการซ่อมสร้างอากาศยาน ให้มีความปลอดภัยและเป็นมาตรฐานสากล



2. According to Weibull data, which of the following is NOT true ?

- a. Complete data is the practitioner is aware of the exact time-to-failure for a sample of the product.
- b. Right Censored data is that all population failed at exact time.
- c. Left Censored data is that the failures are between 0 and 50 hours.
- d. All of the above a, b and c are not true.



Weibull 3 Types of Data

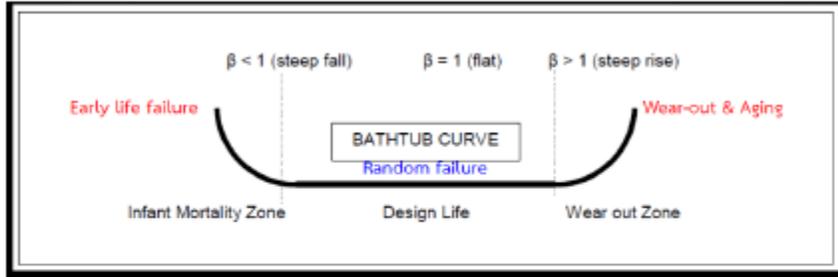
1. Complete data: With Complete data, the practitioner is aware of the exact time-to-failure for a sample of the product. An example would be that the product failed at 15,000 cycles.

2. Right Censored data: With Right Censored data, the practitioner successfully tests the product or component for a pre-determined or known period of time, number of cycles, etc. An example would be that the component operated successfully for 20,000 cycles. The product or component may have continued to perform within acceptable parameters for an unknown period.

3. Interval data and Left Censored data: With these data types, the exact time-to-failure is unknown but it falls within a known time range. An interval is a defined length of time between two known points. Therefore, component failures between 10 and 50 hours of use represent interval data. If the component failures are between 0 and 50 hours, the data is considered left censored.



3. Use the Bathtub Curve to choose the correct answer.

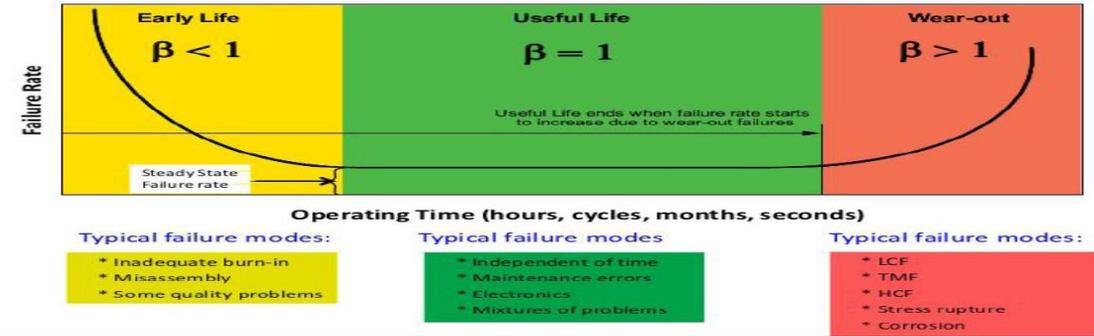


Infant mortality zone is the zone with shape parameter (β) < 1.0; what is the probable cause of infant mortality ?

- a. Inadequate burn in (run in).
- b. Misassemble.
- c. Some quality problems.
- d. All of the above a, b and c are correct.



The Weibull Distribution can describe each portion of the Bathtub curve



β - Shape Parameters Interpretation

$\beta < 1.0$	Infant Mortality	Inadequate burn-in (run-in) time to stress test, production problems, misassemble, poor QC, overhaul problems, solid state electronic failed
$\beta = 1.0$	Random Failures	Maintenance Errors, Human Errors, Abusive Events, FOD, Lightning Strike, Failures due to nature,
$1.0 < \beta < 4.0$	Early Wear Out	Many mechanical failure modes. $\beta = 1.5$: Roller Bearing Failure $\beta = 2.0$: Ball Bearing Failure $\beta = 2.0 - 3.5$: Corrosion or Erosion $\beta = 2.5$: V - Belt Failure $\beta = 2.5 - 4.0$: LCF (Low Cycle Fatigue)
$\beta > 4.0$	Old Age (Rapid) Wear Out	$\beta > 5.0$: Stress Corrosion Material Properties, Brittle materials like ceramics, some form of erosion.



4. Useful life or design life zone is the zone with shape parameter (β) = 1.0; called for random failures; what is the probable cause of random failures?

- a. Maintenance errors.
- b. Operating errors.
- c. Failures due to nature (FOD, Lightning Strike,).
- d. All of the above a, b and c are correct.

β - Shape Parameters Interpretation

$\beta < 1.0$	Infant Mortality	Inadequate burn-in (run-in) time to stress test, production problems, misassemble, poor QC, overhaul problems, solid state electronic failed
$\beta = 1.0$	Random Failures	Maintenance Errors, Human Errors, Abusive Events, FOD, Lightning Strike, Failures due to nature,
$1.0 < \beta < 4.0$	Early Wear Out	Many mechanical failure modes. $\beta = 1.5$: Roller Bearing Failure $\beta = 2.0$: Ball Bearing Failure $\beta = 2.0 - 3.5$: Corrosion or Erosion $\beta = 2.5$: V - Belt Failure $\beta = 2.5 - 4.0$: LCF (Low Cycle Fatigue)
$\beta > 4.0$	Old Age (Rapid) Wear Out	$\beta > 5.0$: Stress Corrosion Material Properties, Brittle materials like ceramics, some form of erosion.



5. Early wear-out zone is the zone with shape parameter $1.0 < \beta < 4.0$; what is the probable cause of early wear out ?

- a. Many mechanical failure modes.
- b. Roller and / or Bearing failures.
- c. V - Belt failures.
- d. All of the above a, b and c are correct.

β - Shape Parameters Interpretation

$\beta < 1.0$	Infant Mortality	Inadequate burn-in (run-in) time to stress test, production problems, misassemble, poor QC, overhaul problems, solid state electronic failed
$\beta = 1.0$	Random Failures	Maintenance Errors, Human Errors, Abusive Events, FOD, Lightning Strike, Failures due to nature,
$1.0 < \beta < 4.0$	Early Wear Out	Many mechanical failure modes. $\beta = 1.5$: Roller Bearing Failure $\beta = 2.0$: Ball Bearing Failure $\beta = 2.0 - 3.5$: Corrosion or Erosion $\beta = 2.5$: V - Belt Failure $\beta = 2.5 - 4.0$: LCF (Low Cycle Fatigue)
$\beta > 4.0$	Old Age (Rapid) Wear Out	$\beta > 5.0$: Stress Corrosion Material Properties, Brittle materials like ceramics, some form of erosion.



6. Old age or rapid wear-out zone is the zone with shape parameter $\beta > 4.0$; what is the probable cause of early wear out ?

- a. Stress corrosion.
- b. LCF (Low Cycle Fatigue), HCF (High Cycle Fatigue), TMF (Thermal Fatigue).
- c. Erosion.
- d. All of the above a, b and c are correct.



$\beta > 4 =$ Wear-out (End of life failures) Directorate Of Aeronautical Engineering

กรมช่างอากาศยาน

- ◆ $\beta > 4$ are wear-out or end of life failures.
- ◆ They should not appear in the design life.
- ◆ Age related failures include stress corrosion cracking, creep, high cycle fatigue (HCF), and erosion.
- ◆ Appropriate maintenance is often **renewal of the item with new** or **send the item to overhaul**.

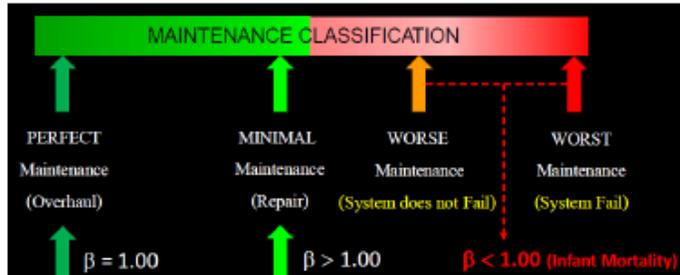
เป็นองค์กรที่มุ่งเน้นการพัฒนาระบบการซ่อมสร้างอากาศยาน ให้มีความปลอดภัยและเป็นมาตรฐานสากล

β - Shape Parameters Interpretation

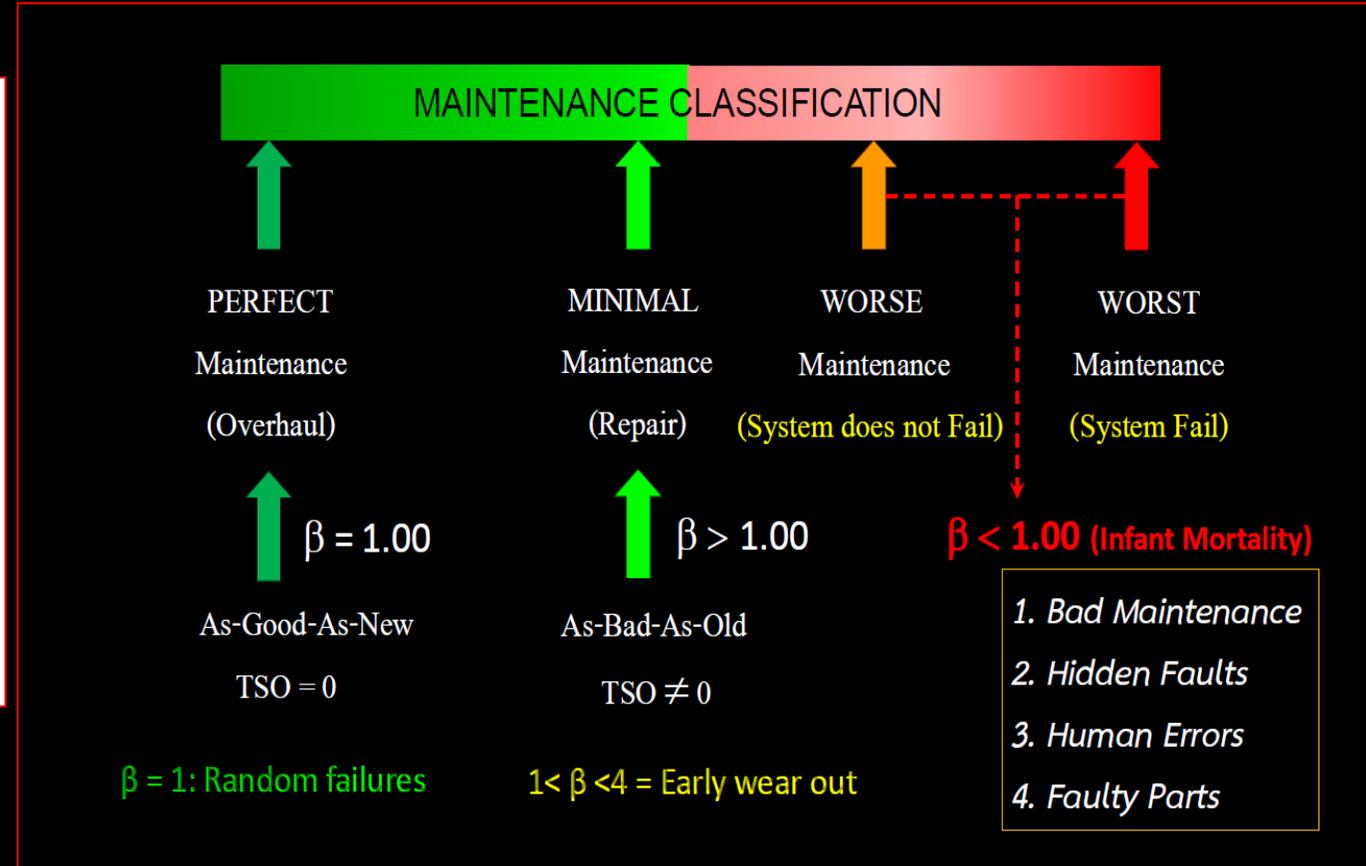
$\beta < 1.0$	Infant Mortality	Inadequate burn-in (run-in) time to stress test, production problems, misassemble, poor QC, overhaul problems, solid state electronic failed
$\beta = 1.0$	Random Failures	Maintenance Errors, Human Errors, Abusive Events, FOD, Lightning Strike, Failures due to nature,
$1.0 < \beta < 4.0$	Early Wear Out	Many mechanical failure modes. $\beta = 1.5$: Roller Bearing Failure $\beta = 2.0$: Ball Bearing Failure $\beta = 2.0 - 3.5$: Corrosion or Erosion $\beta = 2.5$: V - Belt Failure $\beta = 2.5 - 4.0$: LCF (Low Cycle Fatigue)
$\beta > 4.0$	Old Age (Rapid) Wear Out	$\beta > 5.0$: Stress Corrosion Material Properties, Brittle materials like ceramics, some form of erosion.



7. From the maintenance classification figure below, what is the cause of "Worst Maintenance" causing infant mortality ($\beta < 1.0$) ?



- a. Bad maintenance.
- b. Hidden faults.
- c. Human errors and / or use of faulty parts.
- d. All of the above a, b and c are correct.





8. When $\beta = 1.0$, the part implies random failure; overhaul the part is not appropriate for random failure due to independent of time. What type of maintenance is the most effective for parts which have random failures characteristic ?

- a. On Condition (OC)
- b. Condition Monitoring (CM)
- c. System Rate Monitoring (SRM)
- d. Component Reliability Monitoring (CRM)



$\beta = 1$: Random failures

- ◆ $\beta = 1$ implies random failures.
- ◆ These failures are independent of time where an old part is “As good as a New part”.
- ◆ Maintenance overhauls are not appropriate for random failures.
- ◆ Condition monitoring (CM) and inspection are strategies used to detect the onset of failure, and reduce the consequences of failure.
- ◆ This zone is affected by random incidents and accidents.
- ◆ It reflects poor operating procedures, **poor risk management and poor materials selection at design.**

เป็นองค์กรที่มุ่งเน้นการพัฒนาระบบการซ่อมสร้างอากาศยาน ให้มีความปลอดภัยและเป็นมาตรฐานสากล



9. Any Time Change Item (TCI) has its failure rate (λ) = 1 / TBO (Time Between Overhaul). If part "A" has TBO = 2,500 flying hours, what is the failure rate (λ) of part "A" ?

- a. $\lambda_A = 0.0002$ (1/5,000)
- b. $\lambda_A = 0.00025$ (1/4,000)
- c. $\lambda_A = 0.0004$ (1/2,500)
- d. $\lambda_A = 0.0005$ (1/2,000)



แนวทางดำเนินการ (Solution) กรมช่างอากาศยาน
Directorate Of Aeronautical Engineering

1. จากค่าอัตราการชำรุดของพัสดุ หรือ Failure Rate (λ) ที่ได้รับทราบแล้วว่าเป็นค่าคงที่ ($\lambda = \text{Constant}$) “อัตราส่วนของจำนวนพัสดุที่ชำรุดในห้วงเวลาหนึ่ง” โดยที่ค่า Failure Rate (λ) มีค่าคงที่ ($\lambda = \text{Constant}$)
2. ตัวอย่างของ $\lambda = \text{Constant}$ คือพัสดุประเภท TCI (Time Change Item)
3. F100-PW-220/E Core Module เป็นพัสดุ TCI ที่ต้องถอดเปลี่ยนทุก ๆ 4,000 Cycles นั่นคือ OEM กำหนดอายุใช้งานก่อนซ่อมใหญ่ที่ 4,000 Cycles
4. Core Module จึงมีค่า Constant Failure Rate (λ) = 1 / 4,000 = 0.00025
5. เราเรียกว่าเป็นค่าของ “Design Reliability” ของ Core Module ซึ่งคำนวณได้จากสูตร Design Reliability $R(t) = e^{-\lambda * t}$

เป็นองค์กรที่มุ่งเน้นการพัฒนาระบบการซ่อมสร้างอากาศยาน ให้มีความปลอดภัยและเป็นมาตรฐานสากล



10. Any Time Change Item (TCI) has its failure rate (λ) = 1 / TBO (Time Between Overhaul).

Given the design reliability of any part is derived from the formula $R(t) = e^{-\lambda \cdot t}$; t = time.

Then, the design reliability of any TCI at the expired date (t = TBO) shall be

$R(t)_{TCI \text{ expired date}} = e^{-(1/TBO \cdot TBO)} = e^{-1}$. If e = the base for natural logarithms = 2.718281828...

What is the reliability of any TCI at its expired date ?

- a. $1/2.718281828 = 0.37$
- b. $(1 - 1/2.718281828) = 0.63$
- c. $(1/2.718281828) \cdot 2 = 0.74$
- d. $(1/2.718281828) \cdot 1.5 = 0.56$

$$e^{-1} = 1/e = 1/2.718281828$$



แนวทางดำเนินการ (Solution)

1. จากค่าอัตราการชำรุดของพัสดุ หรือ Failure Rate (λ) ที่ได้รับทราบแล้วว่าเป็นค่าคงที่ ($\lambda = \text{Constant}$)
2. ตัวอย่างของ $\lambda = \text{Constant}$ คือพัสดุประเภท TCI (Time Change Item)
3. F100-PW-220/E Core Module เป็นพัสดุ TCI ที่ต้องถอดเปลี่ยนทุก ๆ 4,000 Cycles นั่นคือ OEM กำหนดอายุใช้งานก่อนซ่อมใหญ่ที่ 4,000 Cycles
4. Core Module จึงมีค่า Constant Failure Rate (λ) = $1 / 4,000 = 0.00025$
5. เราเรียกว่าเป็นค่าของ “Design Reliability” ของ Core Module ซึ่งคำนวณได้จากสูตร Design Reliability $R(t) = e^{-\lambda \cdot t}$

เป็นองค์กรที่มุ่งเน้นการพัฒนาระบบการซ่อมสร้างอากาศยาน ให้มีความปลอดภัยและเป็นมาตรฐานสากล



11.

SUMMARY OUTPUT								
Regression Statistics								
Multiple R	0.986493903							
R Square	0.973141152							
Adjusted R Square	0.970174479							
Standard Error	0.176355682							
Observations	31							
ANOVA		df	SS	MS	F	Significance F		
Regression	1	12.13076227	12.13076227	1238.917772	6.5157628			
Residual	29	0.30084352	0.01037398					
Total	30	12.43160579						
	Coefficients	Standard Error	t Stat	P-value	Lower 95%	Upper 95%	Lower 95.0%	Upper 95.0%
Intercept	-9.401431775	0.244340074	-38.811247384	1.49764E-26	-9.983165789	-8.819702164	-9.983165789	-8.819702164
X Variable 1	1.214812056	0.022060871	55.06899081	6.51576E-26	1.147419062	1.282214051	1.147419062	1.282214051
Beta (or Shape Parameter) =	1.214812056							
Alpha (or Characteristic Life) =	2456.222177							

By using Weibull distribution from the figure above, we obtain the value of Shape Parameter (β) = 1.2148 and the value of Characteristic Life (α) = 2,456 flying hours. Which of the following statement is true ?

- The part is normal early wear out ($1.0 < \beta < 4.0$). At 2,456 flying hours, 63 % of the part would be failed and 37 % would be good.
- The part is normal early wear out ($1.0 < \beta < 4.0$). At 2,456 flying hours, 37 % of the part would be failed and 63 % would be good.
- The part is old age wear out ($\beta = 1.2148$). At 2,456 flying hours, 63 % of the part would be failed and 37 % would be good.
- The part is old age wear out ($\beta = 1.2148$). At 2,456 flying hours, 37 % of the part would be failed and 63 % would be good.



$1 < \beta < 4 =$ Early wear out

- $1 < \beta < 4$ implies early wear out.
- You would not expect this type of failure within the design life.
- Failure mechanisms such as corrosion, erosion, low cycle fatigue (LCF) and bearing failures fall in this range.
- Maintenance often involves a periodic rework, modification, retrofit or life extension task.
- The shape can be altered by better materials selection, by degradation management and by good control of operating practices.

เป็นองค์กรที่มุ่งเน้นการพัฒนาระบบการซ่อมสร้างอากาศยาน ให้มีความปลอดภัยและเป็นมาตรฐานสากล



ความหมายของ β และ α

$\beta =$ SHAPE PARAMETER

- $\beta < 1.00$ แสดงว่าเป็นการชำรุดแบบก่อนกำหนด (Infant Mortality)
- $\beta = 1.00$ แสดงว่ามีอัตราการชำรุดที่คงที่ (Constant Failure Rate หรือ $\lambda = 1 / \text{MTBF}$)
- $\beta > 1.00$ แสดงว่าเป็นการชำรุดที่เกิดจากการเสื่อมสภาพจากการใช้งานตามปกติ

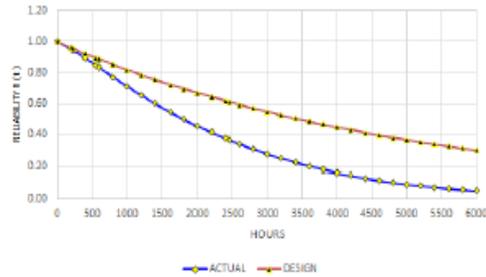
$\alpha =$ CHARACTERISTIC LIFE

- α คือตัวเลขที่บอกถึงอายุใช้งานที่พัสดุจะมีการชำรุด (Failed) = 63.2 % และจะยังมีสภาพใช้งานได้ (Serviceable) = 36.8 % หรือกล่าวอีกนัยหนึ่ง α ก็คือ “อายุใช้งานของพัสดุหลังจากผ่าน Burn-In Period ไปแล้ว จะชำรุดที่อายุเท่าตัวนั่นเอง”

เป็นองค์กรที่มุ่งเน้นการพัฒนาระบบการซ่อมสร้างอากาศยาน ให้มีความปลอดภัยและเป็นมาตรฐานสากล



12.



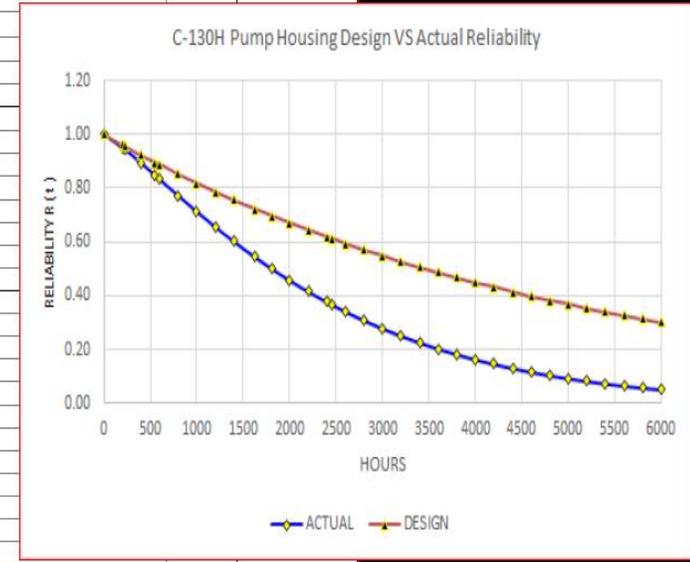
A Time Change Item (TCI) part has its design reliability (orange line) and actual reliability (blue line) as shown in the figure above. The overhaul interval of this TCI part is 5,000 flying hours.

What is the reliability of this TCI at 5,000 flying hours expired ?

- a. 0.74
- b. 0.37
- c. 0.63
- d. 0.56

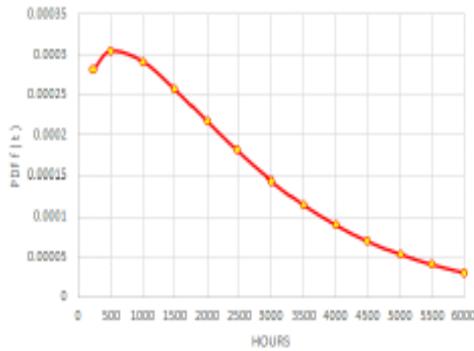


HOURS	ACTUAL RELIABILITY ACTUAL $R = e^{-((t/\alpha)^\beta)}$	DESIGN RELIABILITY $R(t) = e^{-\lambda * t}$		Beta (or Shape Parameter) = 1.214831	TBO
0	1.00000	1.00000		Alpha (or Characteristic Life) = 2456.222	Failure Rate (λ)
200	0.95360	0.96079			
230	0.95	0.95504	WARRANTY		
400	0.89559	0.92312			
550	0.85014	0.89583			
600	0.83489	0.88692			
800	0.77418	0.85214			
1000	0.71487	0.81873			
1200	0.65779	0.78663			
1400	0.60342	0.75578			
1626	0.54561	0.72238			
1816.53	0.50000	0.69537	MEDIAN		
2000	0.45882	0.67032			
2200	0.41697	0.64404			
2400	0.37623	0.61878			
2456.22	0.36788	0.61186	ALPHA (α)		
2600	0.34248	0.59452			
2800	0.30959	0.57121			
3000	0.27943	0.54881			
3200	0.25183	0.52729			
3400	0.22664	0.50662			
3600	0.20370	0.48675			
3800	0.18284	0.46767			
4000	0.16392	0.44933			
4200	0.14678	0.43171			
4400	0.13129	0.41478			
4600	0.11730	0.39852			
4800	0.10469	0.38289			
5000	0.09334	0.36788			
5200	0.08314	0.35345			
5400	0.07398	0.33960			
5600	0.06577	0.32628			
5800	0.05842	0.31349			
6000	0.05185	0.30119			





13. PDF $f(t)$ or Population Density Function of a part has its maximum value at 500 flying hours which has reliability = 0.000304 as shown in the figure below. Which of the following statement is correct ?

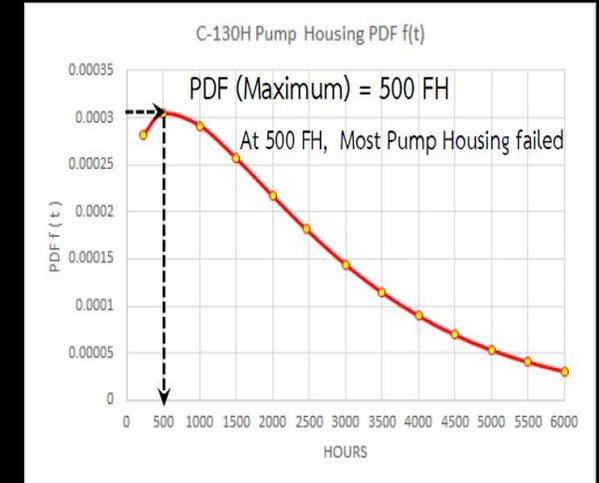


- a. The part would mostly failed at 500 flying hours.
- b. At 500 flying hours, 37 % of the part would be failed and 63 % would be good.
- c. At 500 flying hours, 63 % of the part would be failed and 37 % would be good.
- d. The part would need to be overhauled at 500 flying hours.



11.3 PDF (Population Density Function) Directorate Of Aeronautical Engineering

HOURS	PDF: POPULATION DENSITY FUNCTION: $f(t)$
	PDF: $f(t) = (\beta/t) * (t/\alpha)^\beta * (e^{-(t/\alpha)^\beta})$
230	0.000281084
500	0.000304043
1000	0.000291497
1500	0.000256849
2000	0.00021713
2456.22	0.000181951
3000	0.000144271
3500	0.000114689
4000	9.00272E-05
4500	6.99116E-05
5000	5.37826E-05
5500	4.10304E-05
6000	3.10669E-05





14. What shall we do with parts which have been verified as “Infant Mortality ($\beta < 1.0$)” ?

- Inform MRO provider or MRO supplier of the situation to find root cause(s).
- Inform MRO's Thai Agent of the situation.
- Supply Division and Technical Division record and continue to monitor the situation.
- All of the above a, b and c are correct.



- Weibull เป็นการคำนวณหา **Characteristic Life (α)** ของโครงสร้าง อ., เครื่องยนต์ และบริภัณฑ์ ที่เกิดการชำรุดแบบสุ่ม (Random Failure) มีประโยชน์อย่างยิ่ง เพราะทำให้เราทราบถึงลักษณะของการชำรุด (**β Shape Parameter**) ว่าเป็น Infant Mortality หรือเป็น Normal Wear Out ทำให้ทราบค่า Burn-In Period และทราบอายุใช้งานหลัง Burn-In ว่าเป็นเท่าใด
- กรณีที่พบว่าเป็น Infant Mortality จะได้สืบหาสาเหตุที่เป็น **Root Cause** เช่น คุณภาพของแหล่งซ่อม, คุณภาพของวัสดุที่ใช้ในการซ่อม เป็นต้น
- ขั้นตอนในการดำเนินการไม่ยุ่งยากซับซ้อนอย่างที่คิด ที่สำคัญคือจะต้องทดลองฝึกปฏิบัติบ่อย ๆ จึงจะเกิดความชำนาญ และเป็นการยกระดับขีดความสามารถของหน่วยซ่อมในการคำนวณตามทฤษฎีความเชื่อถือได้ทางวิศวกรรม (Reliability Engineering)

เป็นองค์กรที่มุ่งเน้นการพัฒนากระบวนการซ่อมสร้างอากาศยาน ให้มีความปลอดภัยและเป็นมาตรฐานสากล



15. Ideally, how many data points are required regarding Weibull distribution in order to ensure a robust analysis ?

- a. 5 or more data points.
- b. 10 or less data points.
- c. 10 or more data points.
- d. 5 or less data points.



Weibull Concept

- ◆ Many organizations have kept records of failures manually or in computer systems, **but not used the data in any useful way.**
- ◆ Failure data is the best source of reliability information available.
- ◆ By transforming maintenance and parts history into useful data used to make failure forecasts, **it models the benefits of alternative strategies**, or analyses the reliability of current systems and their capacity to meet operating needs.
- ◆ **Ideally about 10 data points are required** for each failure mode to ensure a robust analysis. Too few points causes uncertainty & interpretation from the curves cannot be trusted.

เป็นองค์กรที่มุ่งเน้นการพัฒนากระบวนการซ่อมสร้างอากาศยาน ให้มีความปลอดภัยและเป็นมาตรฐานสากล



DAE Mobile Training Team

RANDOM FAILURE
(Weibull's Distribution)

TEST & TUTORIAL

As of 5th Feb 2021